Math 1023	College Algebra	Worksheet 2	Name:
	Prof. Paul Bailey	March 1, 2004	

A *quadratic function* is a polynomial of degree two. The *standard form* of a quadratic function is

$$f(x) = ax^2 + bx + c,$$

where a, b, and c are real numbers. The graph is a *parabola* which opens upward if a > 0 and opens downward if a < 0. The y-intercept is the point (0, f(0)), and we see that f(0) = c. The roots of the function are the values of x such that f(x) = 0. The quadratic formula says that f(x) = 0 if and only if

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}.$$

The *discriminant* of the quadratic function is

$$\Delta = b^2 - 4ac;$$

this determines the number of real roots. There are three cases:

(a) if $b^2 - 4ac > 0$, there are two real roots;

- (b) if $b^2 4ac = 0$, there is one real root;
- (c) if $b^2 4ac < 0$, there are no real roots.

The x-intercepts (if any) are the points (x, 0), where x is a real root.

The *shifted form* of a quadratic function is

$$f(x) = a(x-h)^2 + k,$$

where a, h, and k are real numbers. The shifted form tells how the graph of f(x) is obtained from the graph of x^2 , as follows:

- (a) shift horizontally by h;
- (b) stretch vertically by |a|;
- (c) reflect across the x-axis if a is negative;
- (d) shift vertically by k.

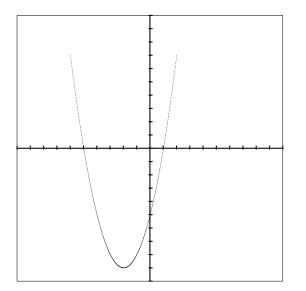
The point (h, k) where the graph turns around is called the *vertex*. Thus k is the *minimum value* of the function if a > 0, and is the *maximum value* of the function is a < 0.

We can convert from standard form to shifted form by completing the square, which leads to:

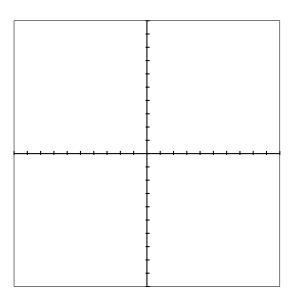
$$h = -\frac{b}{2a}$$
 and $k = c - \frac{b^2}{4a}$

We can convert from shifted form to standard form by squaring and simplifying, which leads to:

$$b = -2ah$$
 and $c = ah^2 + k$.



Example:	$f(x) = 4x - 5 + x^2$
Standard Form:	$x^2 + 4x - 5$
Shifted Form:	$(x+2)^2 - 9$
a: 1 b: 4 c:	-5 h: -2 k: -9
Discriminant:	36
Roots:	x = -5 and $x = 1$
y-intercept:	(0, -5)
x-intercept(s):	(-5,0) and $(1,0)$
Vertex:	(-2, -9)



Problem 1:			$f(x) = x^2 - 6x + 8$				
Standard Form:							
Shifted Form:							
a:	b:	c:	h:	k:			
Discrit	minan	t:					
Roots:							
y-inter	y-intercept:						
<i>x</i> -intercept(s):							
Vertex	Vertex:						

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Problem 2:			$f(x) = (x+2)^2 - 5$				
Standard Form:							
Shifted Form:							
a:	b:	c:		h:	k:		
Discri	minant:						
Roots							
y-inter	y-intercept:						
x-intercept(s):							
Vertex:							

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Problem 3:			$f(x) = 6x \cdot$	$-x^2$	
Standard Form:					
Shifted Form:					
a:	b:	c:	h:	k:	
Discriminant:					
Roots:					
y-intercept:					
<i>x</i> -intercept(s):					
Vertex:					

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Problem 4:	f(f(x) = (3x - 7)(-x + 1)				
Standard Form:						
Shifted Form:						
a: b:	c:	h:	k:			
Discriminant:						
Roots:						
y-intercept:						
x-intercept(s):						
Vertex:						

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Proble	em 5:		$f(x) = 6 + x^2 - 4x$				
Standard Form:							
Shifted Form:							
a:	b:	c:		h:	k:		
Discri	minant:						
Roots	:						
y-inter	y-intercept:						
<i>x</i> -intercept(s):							
Vertex:							